

## Mark scheme for Support Worksheet – Topic 6, Worksheet 3

- 1 a** The energy carried by a wave is distributed along wavefronts; if we consider a very low intensity beam of light incident on the metal the energy is being delivered to the metal at a very low rate and so the time required for the electron to accumulate the energy needed to escape would be very large. [2]
- b** According to the photon theory of light, the energy of light is carried by individual photons; and the entire energy carried by the photon is transferred to the electron at once when the photon is absorbed. [2]
- 2 a** (Whereas the energy carried by mechanical waves depends on both frequency and amplitude) the energy carried by electromagnetic waves depends only on the amplitude and not the frequency; hence the energy of the emitted electron cannot have any dependence on frequency. [2]
- b** According to the photon theory the energy of a photon is given by  $hf$ ; hence the energy of the emitted electron is  $hf - \phi$  and so depends on the light frequency. [2]
- 3 a** The intensity has no effect on the energy of the electrons; increased intensity implies more photons not more energetic photons. [2]
- b** More electrons would be ejected; increased intensity implies more photons and hence greater probability for more electrons to be ejected from the metal. [2]
- 4** The work function is the minimum energy required to eject an electron from a metal surface. [1]
- 5** 
$$E_K = hf - \phi = \frac{hc}{\lambda} - \phi = \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{4.2 \times 10^{-7}} - 2.2 \times 1.6 \times 10^{-19}$$

$$= 1.00 \times 10^{-19} \text{ J}$$
- $$\frac{1}{2}mv^2 = 1.00 \times 10^{-19} \text{ J} \Rightarrow v = \sqrt{\frac{2.00 \times 10^{-19}}{9.1 \times 10^{-31}}} = 4.7 \times 10^5 \text{ m s}^{-1}$$
 [3]
- 6 a** Stopping voltage is that voltage between the anode and the cathode in a photoelectric effect experiment for which the photocurrent becomes zero. [1]
- b** From  $eV_s = hf - \phi \Rightarrow V_s = \frac{hf}{e} - \frac{\phi}{e}$  the slope is  $\frac{h}{e}$ , i.e. Planck's constant divided by the elementary charge. [1]
- 7 a** Particles show wavelike behaviour; with a wavelength that equals Planck's constant divided by the particle's momentum. [2]
- b** See *Physics for the IB Diploma*, pages 394–395. [3]

**8**  $\frac{p^2}{2m} = 150 \times 1.6 \times 10^{-19} \Rightarrow p = 6.61 \times 10^{-24} \text{ N s};$  and so

$$\lambda = \frac{h}{p} = \frac{6.63 \times 10^{-34}}{6.61 \times 10^{-24}} = 1.0 \times 10^{-10} \text{ m}$$

[2]

**9 a** The allowed wavelengths are  $\lambda = \frac{2L}{n}$  with  $n = 1, 2, 3, \dots$

[1]

**b**  $E = \frac{p^2}{2m} = \frac{h^2}{2m\lambda^2};$  and so  $E = \frac{h^2}{2m\left(\frac{2L}{n}\right)^2} = \frac{h^2 n^2}{8mL^2}$

[2]

**10 a** The product of the uncertainties in momentum and position is never less than Planck's constant divided by  $4\pi$ .

[1]

**b** Since  $\Delta x : 10^{-10} \text{ m}$  (this is an order of magnitude calculation so you may choose  $\Delta x : \frac{1}{2} \times 10^{-10} \text{ m}$  if you wish);

$$\Delta p \approx \frac{h}{4\pi\Delta x} = \frac{6.63 \times 10^{-34}}{4\pi \times 10^{-10}} = 5.3 \times 10^{-25} \approx 10^{-24} \text{ N s}$$

[2]