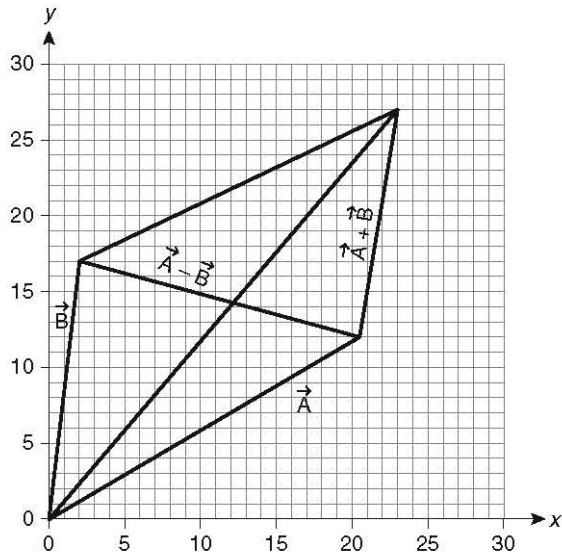


Answers to Coursebook questions – Chapter 1.4

1



2 a



Scale: 1 unit = 1 cm

$\vec{A} + \vec{B}$

length 18 cm

$F \approx 18$ units

$\theta \approx 49^\circ$

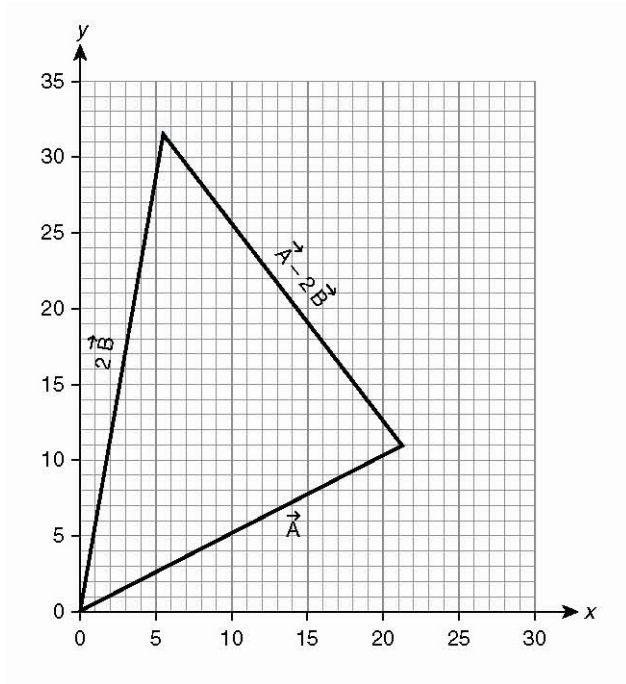
b $\vec{A} - \vec{B}$

length 9.5 cm

$F \approx 9.5$ units

$\theta \approx 11^\circ$ below horizontal.

c



Scale: 1 unit = 1 cm

$$\vec{A} + \vec{B}$$

length 13 cm

$F \approx 13$ units

$\theta \approx 42^\circ$ below horizontal.



3 The components are:

$$A_x = 12 \times \cos 30^\circ = 10.39$$

$$B_x = 8.00 \times \cos 80^\circ = 1.389$$

$$A_y = 12 \times \sin 30^\circ = 6.00$$

$$B_y = 8.00 \times \sin 80^\circ = 7.878$$

a $(A + B)_x = 10.39 + 1.389 = 11.799$

$$(A + B)_y = 6.00 + 7.878 = 13.878$$

The vector $\vec{A} + \vec{B}$ has magnitude $\sqrt{11.799^2 + 13.878^2} = 18.2$ and is directed at an angle $\theta = \arctan \frac{13.878}{11.799} = 49.6^\circ$ to the horizontal.

b $(A - B)_x = 10.39 - 1.389 = 9.001$

$$(A - B)_y = 6.00 - 7.878 = -1.878$$

The vector $\vec{A} - \vec{B}$ has magnitude $\sqrt{9.001^2 + 1.878^2} = 9.19$ and is directed at an angle $\theta = \arctan \left(-\frac{1.878}{9.001} \right) = -11.8^\circ$ below the horizontal.

c $(A - 2B)_x = 10.39 - 2 \times 1.389 = 7.612$

$$(A - 2B)_y = 6.00 - 2 \times 7.878 = -9.756$$

The vector $\vec{A} - 2\vec{B}$ has magnitude $\sqrt{7.612^2 + 9.756^2} = 12.4$ and is directed at an angle $\theta = \arctan \left(-\frac{9.756}{7.612} \right) = -52.0^\circ$ below the horizontal.

4 The components of her change of displacement in each leg of the walk are:

$$d_{1x} = -5.0 \text{ km}$$

$$d_{1y} = 0$$

$$d_{2x} = 0$$

$$d_{2y} = +3.0 \text{ km}$$

$$d_{3x} = 2.0 \cos 45^\circ = 1.41 \text{ km}$$

$$d_{3y} = 2.0 \sin 45^\circ = 1.41 \text{ km}$$

Therefore her displacement from the starting point is

$$d_x = -5.0 + 0 + 1.41 = -3.59 \text{ km} \quad \text{and} \quad d_y = 0 + 3.0 + 1.41 = +4.41 \text{ km}$$

Her distance is the magnitude of the displacement vector, i.e. $d = \sqrt{3.59^2 + 4.41^2} = 5.69 \text{ km}$

in a direction $\theta = 180^\circ - \arctan \frac{4.41}{3.59} = 129^\circ$.

(Notice that her position is in the second quadrant.)

5 a $\sqrt{4.0^2 + 4.0^2} = 5.66 \text{ cm}$ in a direction $\theta = 180^\circ + \arctan \frac{4.0}{4.0} = 225^\circ$.

b $\sqrt{124^2 + 158^2} = 201 \text{ km}$ in a direction $\theta = \arctan \left(-\frac{158}{124} \right) = -52^\circ$.

c $\sqrt{0^2 + 5.0^2} = 5.0 \text{ m}$ in a direction $\theta = 270^\circ$ or $\theta = -90^\circ$.

d $\sqrt{8.0^2 + 0^2} = 8.0 \text{ N}$ in a direction $\theta = 0^\circ$.

6 a $\sqrt{2.00^2 + 3.00^2} = 3.61$ at $\theta = \arctan \frac{3.00}{2.00} = 56.3^\circ$.

b $\sqrt{2.00^2 + 5.00^2} = 5.39$ at $\theta = 180^\circ - \arctan \frac{5.00}{2.00} = 112^\circ$.

c $\sqrt{0^2 + 8.00^2} = 8.00$ at $\theta = 90^\circ$

d $\sqrt{4.00^2 + 2.00^2} = 4.47$ at $\theta = \arctan \left(-\frac{2.00}{4.00} \right) = -26.6^\circ$.

e $\sqrt{6.00^2 + 1.00^2} = 6.08$ at $\theta = \arctan \frac{1.00}{6.00} = 9.46^\circ$.

7 The vector \vec{C} is given by $\vec{C} = \vec{B} - \vec{A}$. Its components are

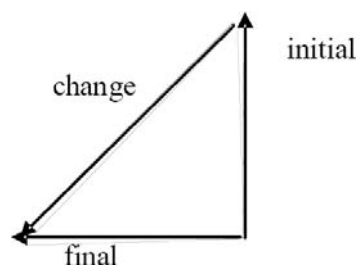
$$C_x = -1.00 - 3.00 = -4.00 \text{ cm} \quad C_y = 5.00 - 4.00 = +1.00 \text{ cm}$$

Hence the magnitude is $\sqrt{4.00^2 + 1.00^2} = 4.12$ in a direction $\theta = 180^\circ - \arctan \frac{1}{4} = 166^\circ$.

The vector is in the second quadrant.

8 The change in displacement has components $\Delta r_x = 4 - 2 = 2$, $\Delta r_y = 8 - 2 = 6$.

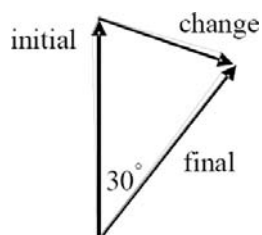
9 A diagram is



The magnitude of the change in the velocity vector is $\sqrt{10^2 + 10^2} = 14.1 \text{ m s}^{-1}$.

The vector makes an angle of 45° with the horizontal as shown in the diagram.

- 10 A diagram is:



The other two angles of the triangle are each $\frac{1}{2}(180^\circ - 30^\circ) = 75^\circ$.

Using the same rule we find:

$$\frac{\Delta p}{\sin 30^\circ} = \frac{p}{\sin 75^\circ} \Rightarrow \Delta p = p \times \frac{\sin 30^\circ}{\sin 75^\circ} = 0.518p \approx 0.52p$$

11 a $(x_2 - x_1, y_2 - y_1)$

b $(x_1 - x_2, y_1 - y_2)$

c $\sqrt{x_1^2 + y_1^2}$

- 12 The components of the velocity vector at the various points are:

A: $v_{Ax} = -4.0 \text{ m s}^{-1}$ $v_{Ay} = 0$

B: $v_{Bx} = +4.0 \text{ m s}^{-1}$ $v_{By} = 0$

C: $v_{Cx} = 0$ $v_{Cy} = 4.0 \text{ m s}^{-1}$

- a From A to B the change in the velocity vector has the components

$$v_{Bx} - v_{Ax} = +4.0 - (-4.0) = 8.0 \text{ m s}^{-1} \text{ and } v_{By} - v_{Ay} = 0 - 0 = 0.$$

- b From B to C the change in the velocity vector has the components

$$v_{Cx} - v_{Bx} = 0 - 4.0 = -4.0 \text{ m s}^{-1} \text{ and } v_{Cy} - v_{By} = 4.0 - 0 = 4.0 \text{ m s}^{-1}.$$

- c From A to C the change in the velocity vector has the components

$$v_{Cx} - v_{Ax} = 0 - (-4.0) = 4.0 \text{ m s}^{-1} \text{ and } v_{Cy} - v_{Ay} = 4.0 - 0 = 4.0 \text{ m s}^{-1}.$$

The change in the vector from A to C is the sum of the change from A to B and the change from B to C.

- 13 a The initial velocity is $+352 \text{ m s}^{-1}$ and the final velocity after the collision is -352 m s^{-1} . The change in the velocity is therefore $-352 - 352 = -704 \text{ m s}^{-1}$.
- b The speed is the same before and after the collision, so the change in speed is zero.

- 14 a $A_x = -10.0\cos 40^\circ = -7.66$ $A_y = -10.0\sin 40^\circ = +6.43$
 b $A_x = -10.0\cos 35^\circ = -8.19$ $A_y = -10.0\sin 35^\circ = -5.74$
 c $A_x = +10.0\cos 68^\circ = +3.75$ $A_y = -10.0\sin 68^\circ = -9.27$
 d $A_x = +10.0\cos(90^\circ - 48^\circ) = +7.43$ $A_y = -10.0\sin(90^\circ - 48^\circ) = -6.69$
 e $A_x = -10.0\cos(90^\circ - 30^\circ) = -5.00$ $A_y = -10.0\sin(90^\circ - 30^\circ) = -8.66$

- 15 The vector we want is $\vec{C} = -(\vec{A} + \vec{B})$. The components of \vec{A} and \vec{B} are:

$$A_x = 6.0\cos 60^\circ = +3.0$$

$$A_y = 6.0\sin 60^\circ = +5.20$$

$$B_x = 6.0\cos 120^\circ = -3.0$$

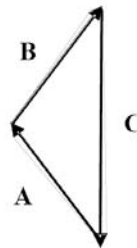
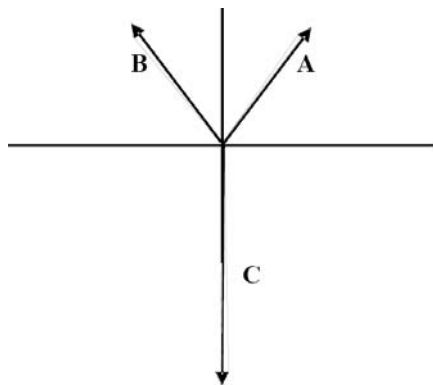
$$B_y = 6.0\sin 120^\circ = +5.20$$

So,

$$C_x = -(+3.0 - 3.0) = 0$$

$$C_y = -(+5.20 + 5.20) = -10.4$$

The magnitude of vector \vec{C} is therefore 10.4 and is directed along the negative y -axis.





16 a $A_x = 12.0\cos 20^\circ = +11.28$ and $A_y = 12.0\sin 20^\circ = +4.10$.

$$B_x = 14.0\cos 50^\circ = +9.00 \text{ and } B_y = 14.0\sin 50^\circ = +10.72.$$

The sum has the components:

$$S_x = +11.28 + 9.00 = 20.28 \text{ and } S_y = +4.10 + 10.72 = 14.82.$$

$$\text{The magnitude of the sum is } \sqrt{20.28^2 + 14.82^2} = 25.1$$

$$\text{and its direction is } \theta = \arctan \frac{14.82}{20.28} = 36.2^\circ.$$

b $A_x = 15.0\cos 15^\circ = +14.49$ and $A_y = 15.0\sin 15^\circ = +3.88$.

$$B_x = 18.0\cos 105^\circ = -4.66 \text{ and } B_y = 18.0\sin 105^\circ = +17.39.$$

The sum has the components:

$$S_x = +14.49 - 4.66 = 9.83 \text{ and } S_y = +3.88 + 17.39 = 21.27.$$

$$\text{The magnitude of the sum is } \sqrt{9.83^2 + 21.27^2} = 23.4 \text{ and its direction is } \theta = \arctan \frac{21.27}{9.83} = 65.2^\circ.$$

c $A_x = 20.0\cos 40^\circ = +15.32$ and $A_y = 20.0\sin 40^\circ = +12.86$.

$$B_x = 15.0\cos 310^\circ = +9.64 \text{ and } B_y = 15.0\sin 310^\circ = -11.49.$$

The sum has components:

$$S_x = +15.32 + 9.64 = 24.96 \text{ and } S_y = +12.86 - 11.49 = +1.37.$$

$$\text{The magnitude of the sum is } \sqrt{24.96^2 + 1.37^2} = 25.0 \text{ and its direction is } \theta = \arctan \frac{1.37}{24.96} = 3.14^\circ.$$